

CURRENT:

FLOW OF CHARGE ACROSS A SURFACE

UNIT: AMPERE $\rightarrow 1 \text{ A} = 1 \text{ COULOMB/S}$

FUNDAMENTAL CHARGE $e \sim 1.6e^{-19} \text{ C}$

SPROTT

$$I = \frac{dQ}{dt}$$

VOLTAGE: ELECTRICAL POTENTIAL DIFFERENCE

$$1 \text{ V} = 1 \text{ JOULE/COULOMB}$$

APPLY VOLTAGE DIFFERENCE BETWEEN 2 POINTS;
CURRENT WILL FLOW

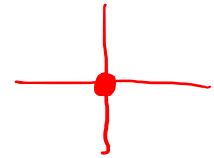
$$I = V/R \rightarrow \text{RESISTANCE; DETERMINED BY GEOMETRY, MATERIALS, TEMPERATURE [PHONON, IMPURITY SCATTERING]}$$

OHM'S LAW

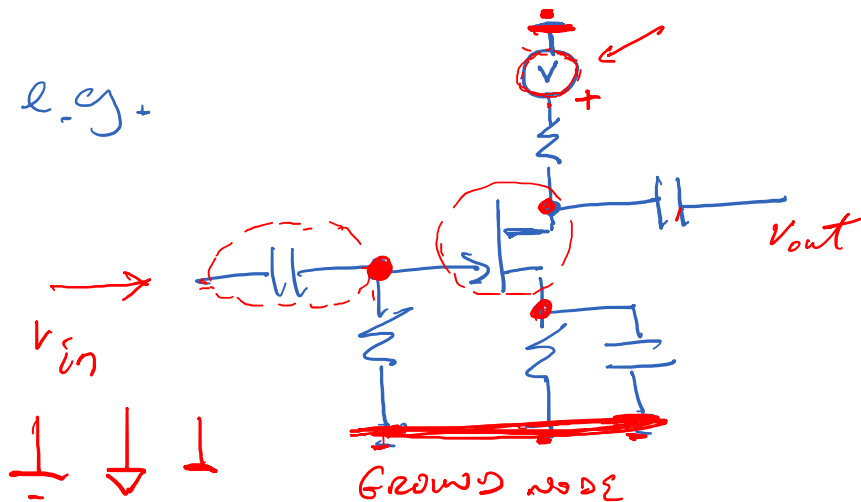
CONDUCTANCE $G \equiv 1/R$

ELECTRICAL CIRCUIT; NETWORK OF NODES
JOINED BY BRANCHES

VOLTAGES @ NODES,
CURRENTS THRU BRANCHES



e.g.



CIRCUIT INCLUDING
SOURCE,

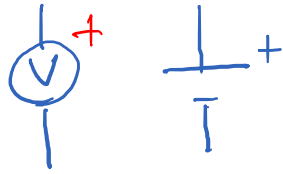
IMPEDANCES,

3-TERMINAL ACTIVE ELEMENT
(n-CHANNEL JFET)

CURRENT FLOW ACROSS A POTENTIAL DROP DISSIPATES POWER
[ASSUMING $I \neq V$ ARE IN PHASE: MORE ON THIS LATER]

$$\underline{P = IV = I^2 R = \frac{V^2}{R}}$$

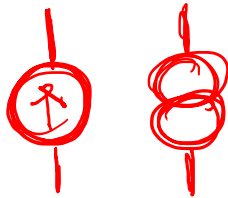
VOLTAGE SOURCE



IDEAL: SUPPLIES A CONSTANT VOLTAGE,
REGARDLESS OF CURRENT THROUGH IT

[i.e., IDEAL V. SOURCE HAS ZERO INTERNAL RESISTANCE]

CURRENT SOURCE

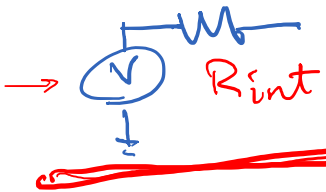


IDEAL: SUPPLIES CONSTANT CURRENT,
REGARDLESS OF VOLTAGE ACROSS IT

[i.e., IDEAL I SOURCE HAS INFINITE INTERNAL RESISTANCE]

PRACTICAL SOURCES

V. SOURCE CAN BE MODELLED AS IDEAL SOURCE IN SERIES W/ INTERNAL RESISTANCE



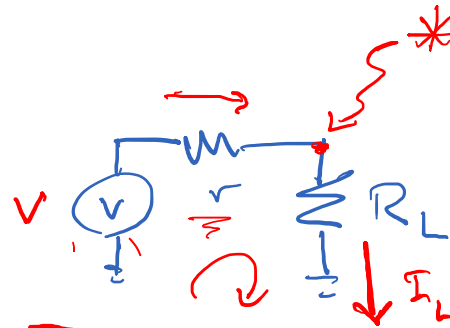
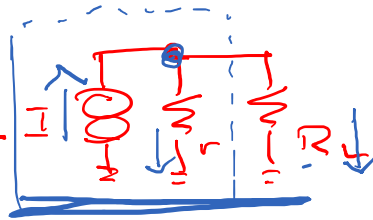
CONNECT TO LOAD R_L :

sum

I. SOURCE CAN BE MODELLED AS IDEAL SOURCE IN PARALLEL W/ INTERNAL RESISTANCE



CONNECT TO LOAD



$$I_L = \frac{V}{r + R_L}$$

$$V_L = I_L \cdot R_L$$

$$V_L = \frac{R_L}{r + R_L} V \approx V$$

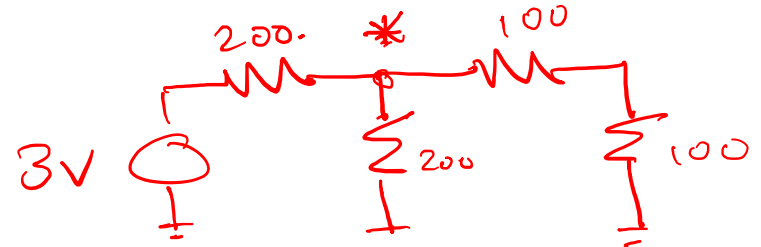
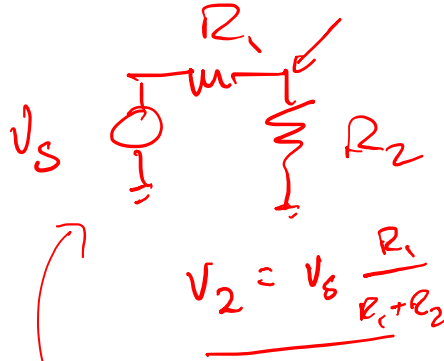
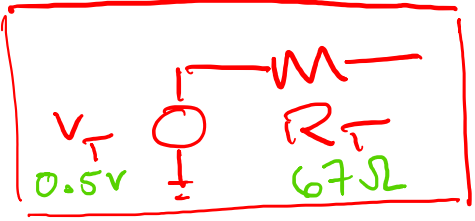
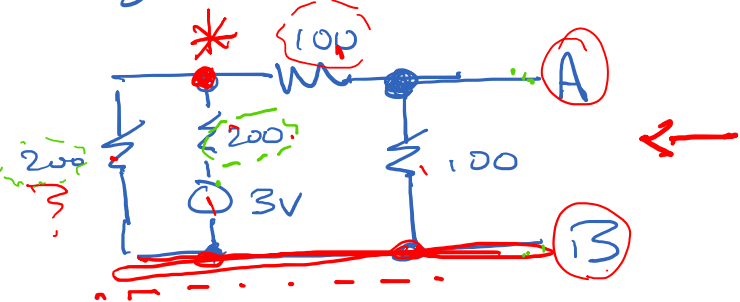
PROVIDED $R_L \gg r$

$$I_L = I \frac{\frac{1}{R_L}}{\frac{1}{R_L} + \frac{1}{r}} = \frac{I r}{r + R_L}$$

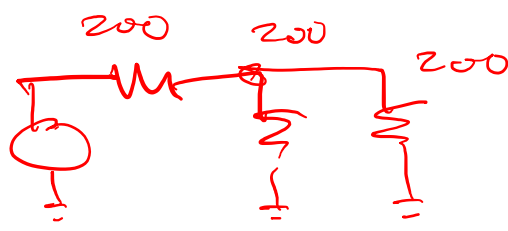
$I_L \approx I$, PROVIDED $r \gg R_L$

THEVENIN TH'M: ANY LINEAR, 2-TERMINAL NETWORK CAN BE EXPRESSED AS A VOLTAGE SOURCE IN SERIES WITH A RESISTOR (IMPEDANCE)

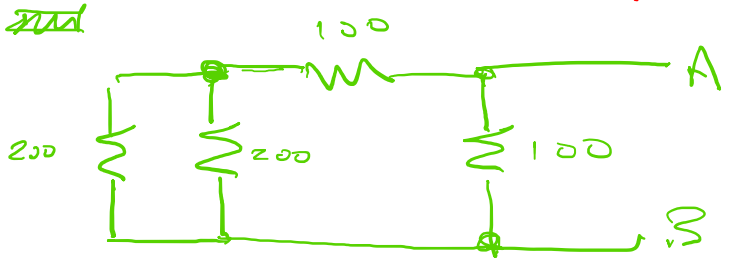
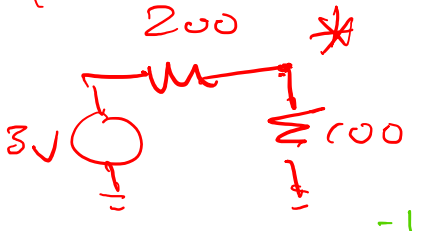
e.g.



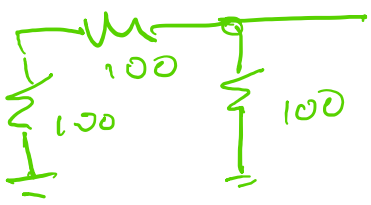
=>



=>



=>



=>

$R_T = 67\Omega$

$$R_{||} = \left[\frac{1}{R_1} + \frac{1}{R_2} \right]^{-1}$$

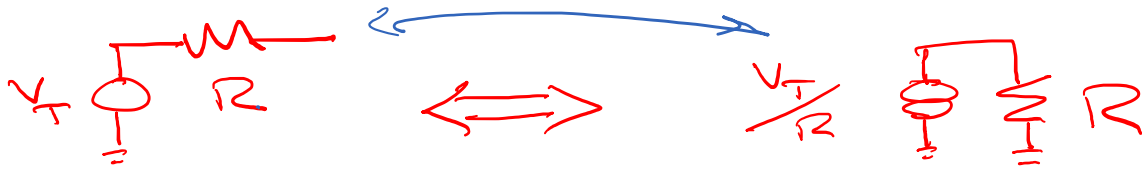
NORTON TH'M:

ANY LINEAR, 2-TERMINAL NETWORK CAN BE EXPRESSED AS IDEAL CURRENT SOURCE IN PARALLEL WITH A RESISTOR [IMPEDANCE]

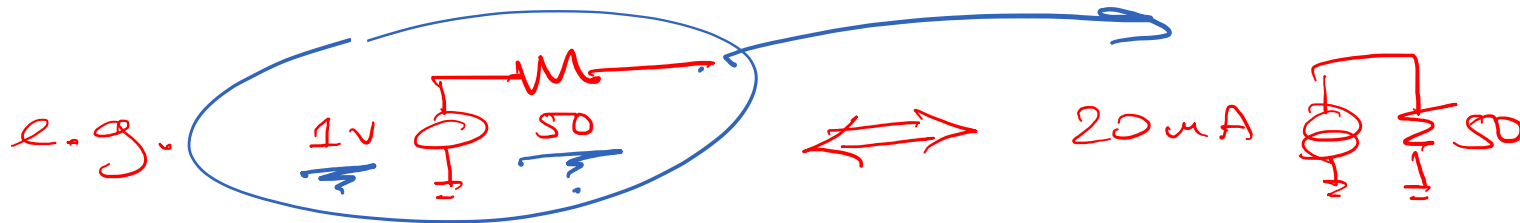
TO DETERMINE THEVENIN / NORTON EQUIVALENT, MEASURE V_{oc} [OPEN CIRCUIT] & I_{sc} [SHORT CIRCUIT]

THEVENIN

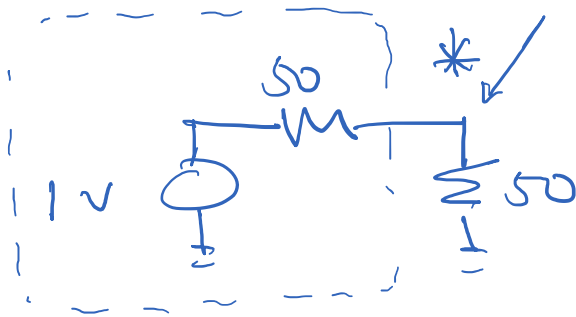
THEVENIN - NORTON TRANSFORMATION:



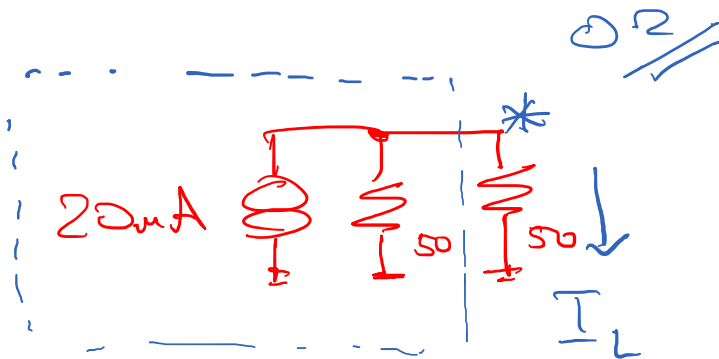
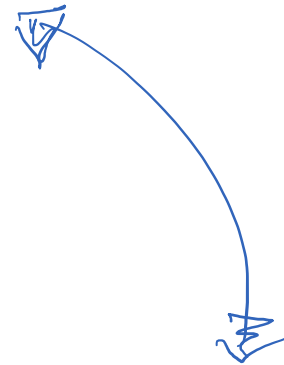
$$I_N = \frac{V_T}{R_T} = \frac{1V}{50\Omega} = 20\mu A$$



CONSIDER 50Ω LOADS



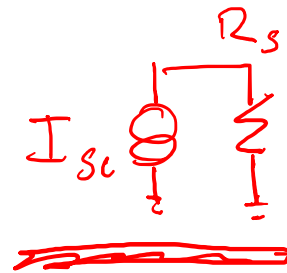
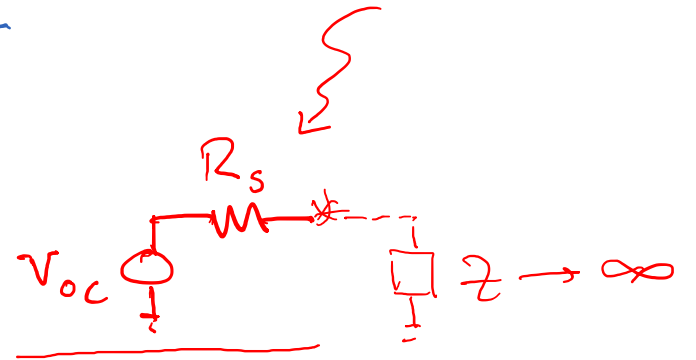
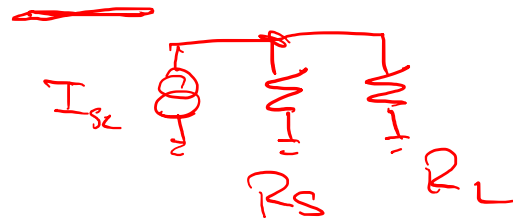
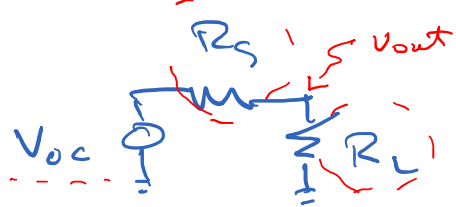
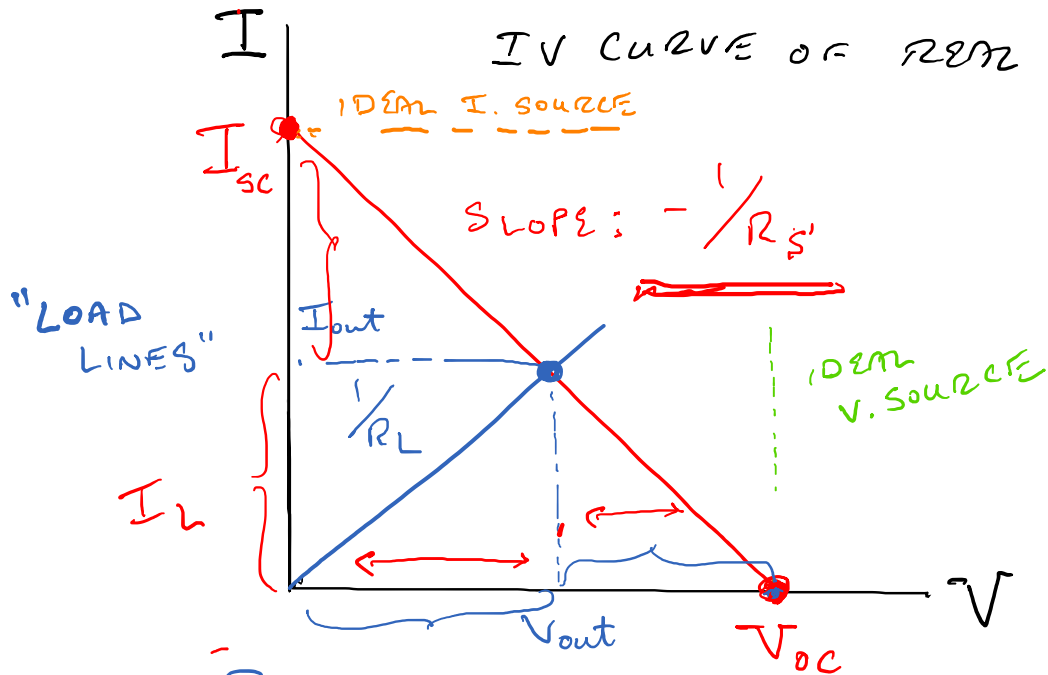
$$V_* = 0.5V$$



$$V_* = I_L \cdot 50\Omega$$
$$= 10mA \cdot 50\Omega = \underline{0.5V}$$

THEVENIN - NORTON EQUIVALENCE

IV CURVE OF REAL SOURCE



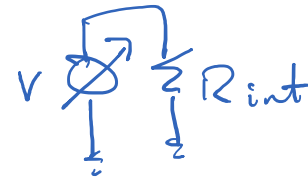
$$R_s = \frac{V_{oc}}{I_{sc}}$$

METERS

VOLTMETER : CONNECT ACROSS 2 NODES

IDEAL : INFINITE INTERNAL IMPEDANCE

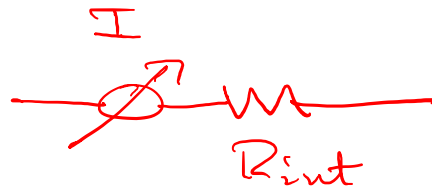
PRACTICAL V. METER MODELLED AS IDEAL METER
IN PARALLEL w/ FINITE INTERNAL IMPEDANCE



AMMETER : INSERT INTO A BRANCH

IDEAL : ZERO INTERNAL RESISTANCE

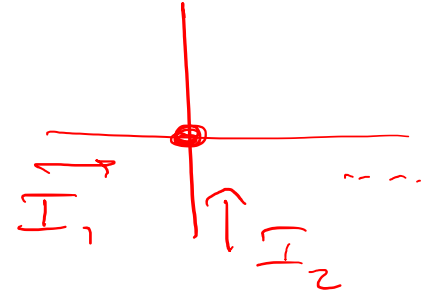
PRACTICAL AMMETER MODELLED AS IDEAL METER
IN SERIES w/ NONZERO INTERNAL RESISTANCE



CIRCUIT THEOREMS

KIRCHOFF'S LAWS

- SUM OF CURRENTS FLOWING INTO A NODE IS ZERO
[CONSERVATION OF CHARGE]



- - SUM OF VOLTAGE DROPS AROUND A CLOSED LOOP IS ZERO
[CONSERVATION OF ENERGY]

CIRCUIT TH'MS, CONT'D

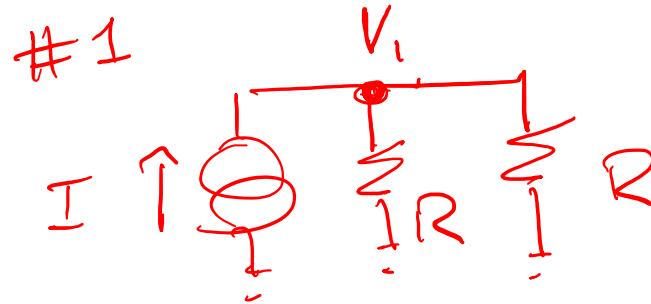
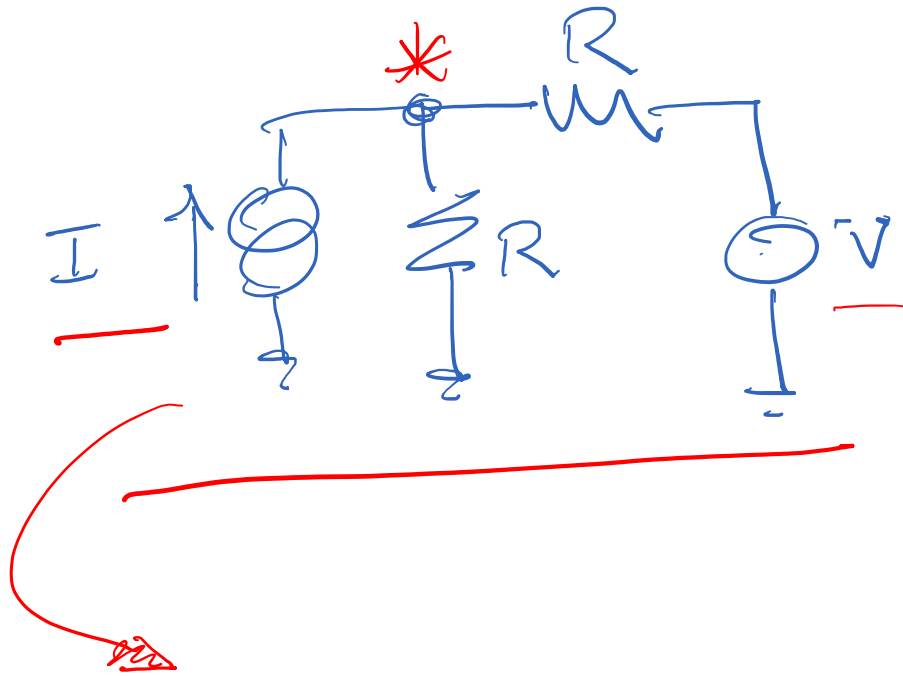
SUPERPOSITION TH'M

IN A CIRCUIT w/ MULTIPLE SOURCES,
CURRENT IN A BRANCH [VOLTAGE @ A NODE]
IS THE SUM OF CURRENTS [VOLTAGES]
PRODUCED BY EACH SOURCE SEPARATELY,
WITH OTHER SOURCES REPLACED BY
THEIR INTERNAL RESISTANCES

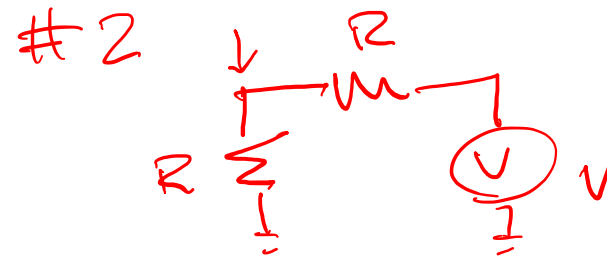
HOLDS FOR LINEAR CIRCUITS

ALLOWS US TO CALCULATE RESPONSE OF
A CIRCUIT TO ARBITRARY DRIVE WAVEFORM
USING FOURIER DECOMPOSITION & CONCEPT OF
FREQUENCY-DEPENDENT IMPEDANCE

EXAMPLE



$$V_1 = I \cdot \frac{R}{2}$$



$$V_2 = \frac{V}{2}$$

$$V_* = \frac{1}{2} I R + \frac{V}{2}$$