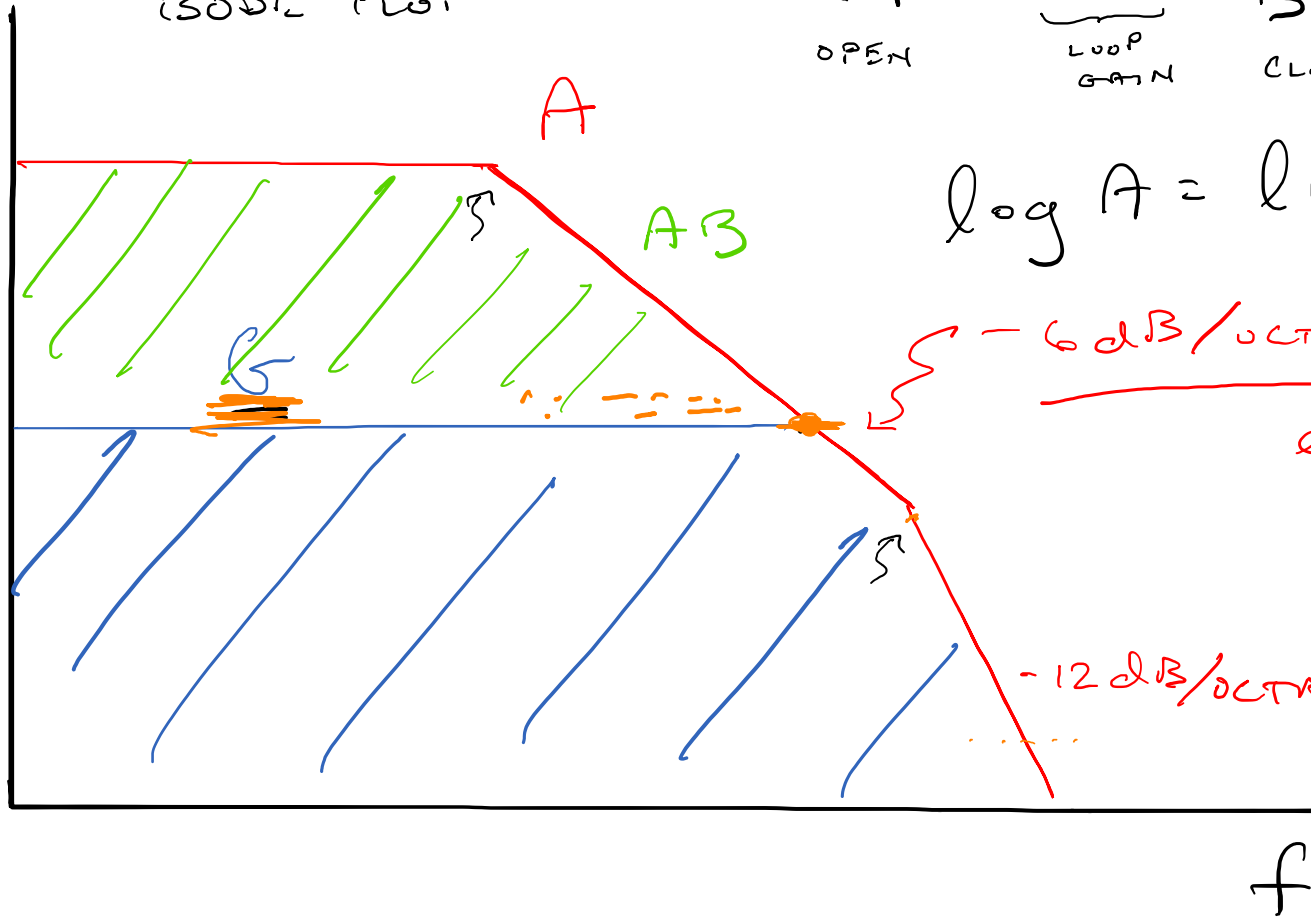


# OP AMP STABILITY

"BODE PLOT"



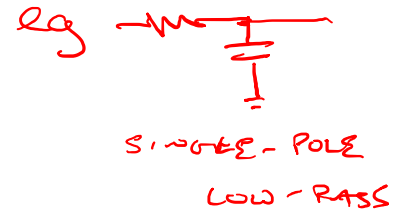
$$A = \underbrace{(AB)}_{\text{LOOP GAIN}} \frac{1}{\beta} = (AB) G$$

OPEN
CLOSED

$$\log A = \log (AB) + \log G$$

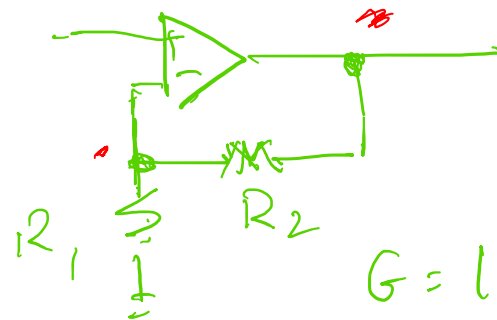
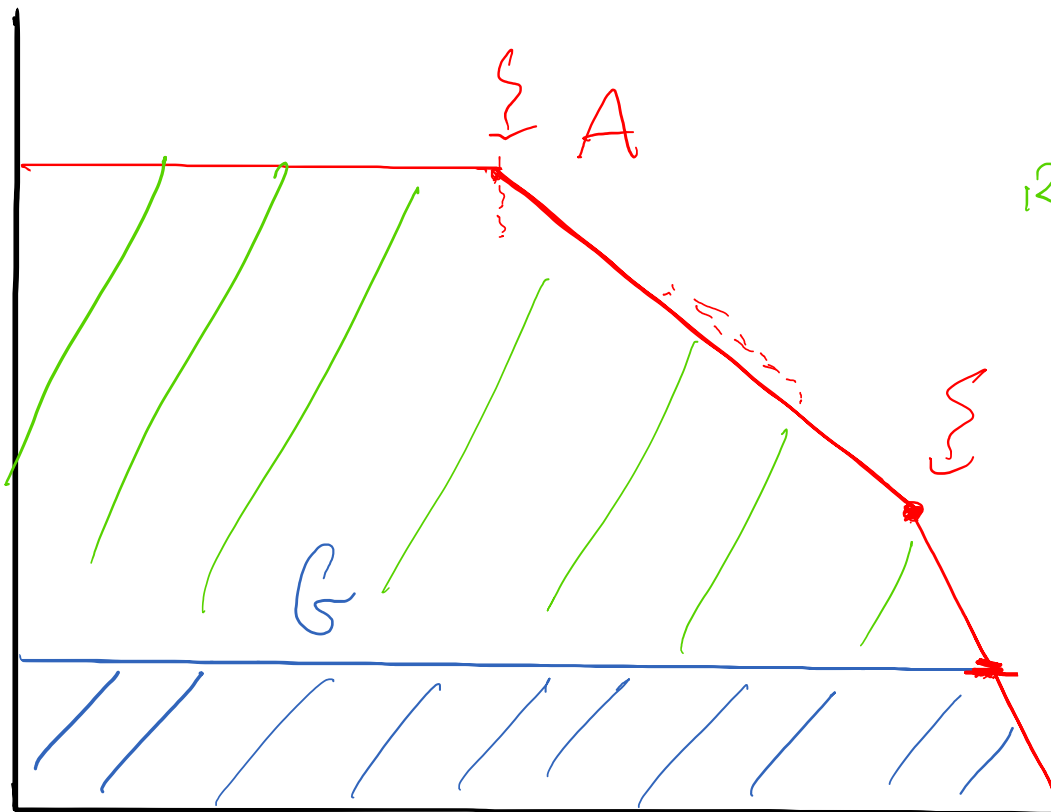
GAIN  
 e.g.  $10 \log_{10} |A|^2$

-6 dB/OCTAVE



-12 dB/OCTAVE.

# OP AMP STABILITY



$$G = 1 + \frac{R_2}{R_1}$$

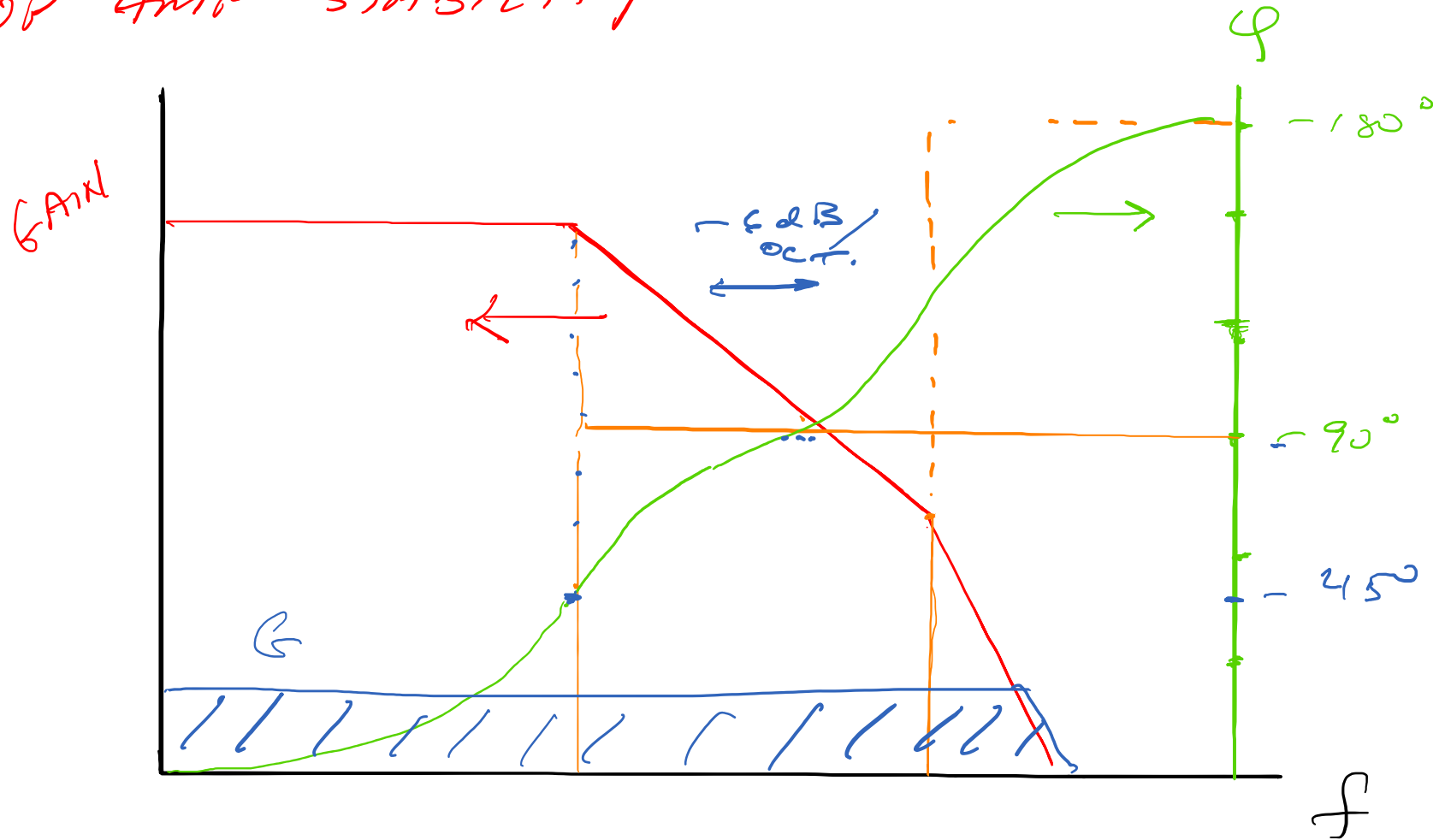
"PHASE MARGIN"

HOW FAR ACCUM. PHASE  
IN FB LOOP IS FROM  
 $-180^\circ$  @ POINT  
WHERE LOOP GAIN  
 $= 1$ .

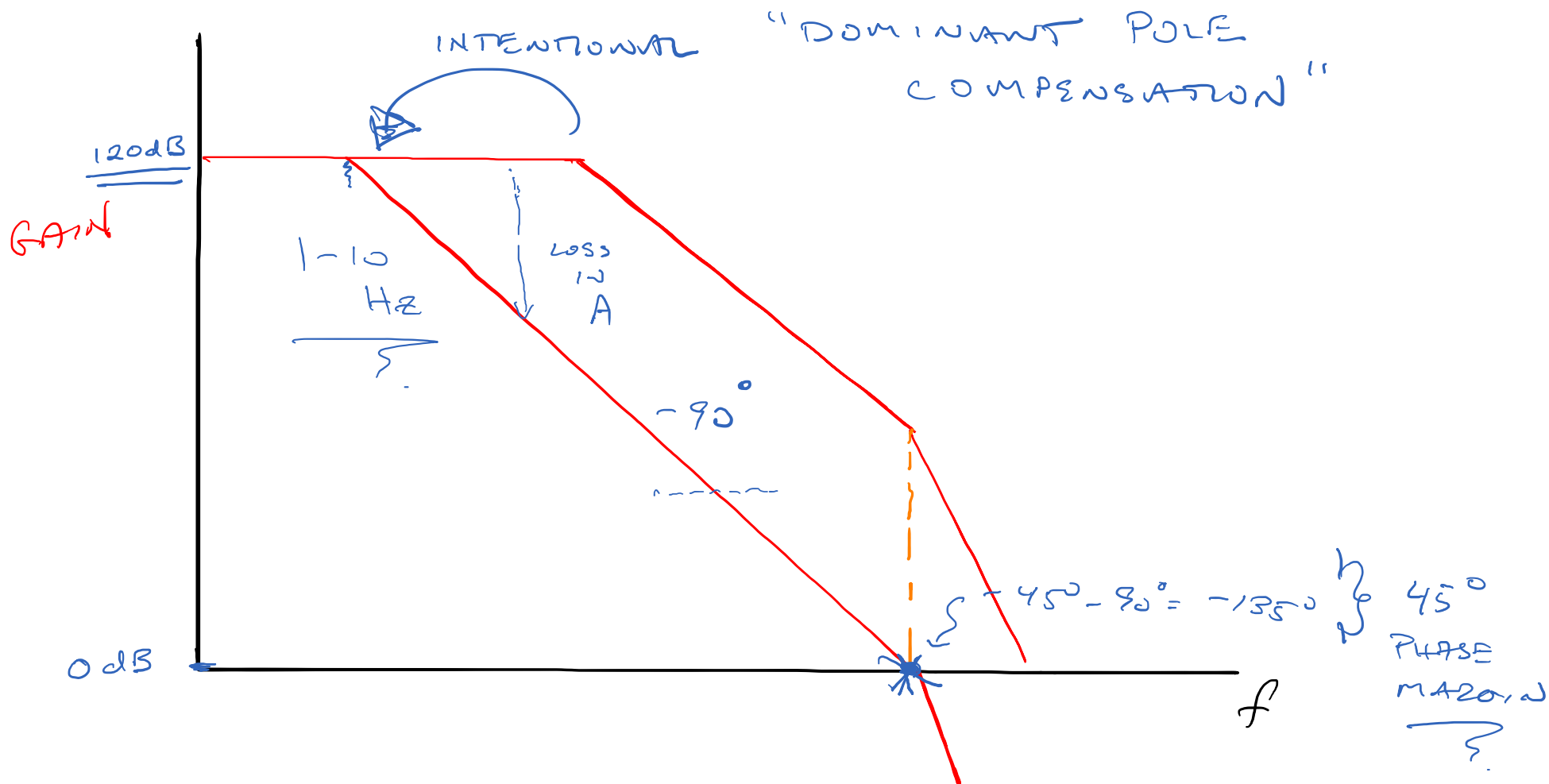
WORST CASE:

FOLLOWER:  $G = 1$

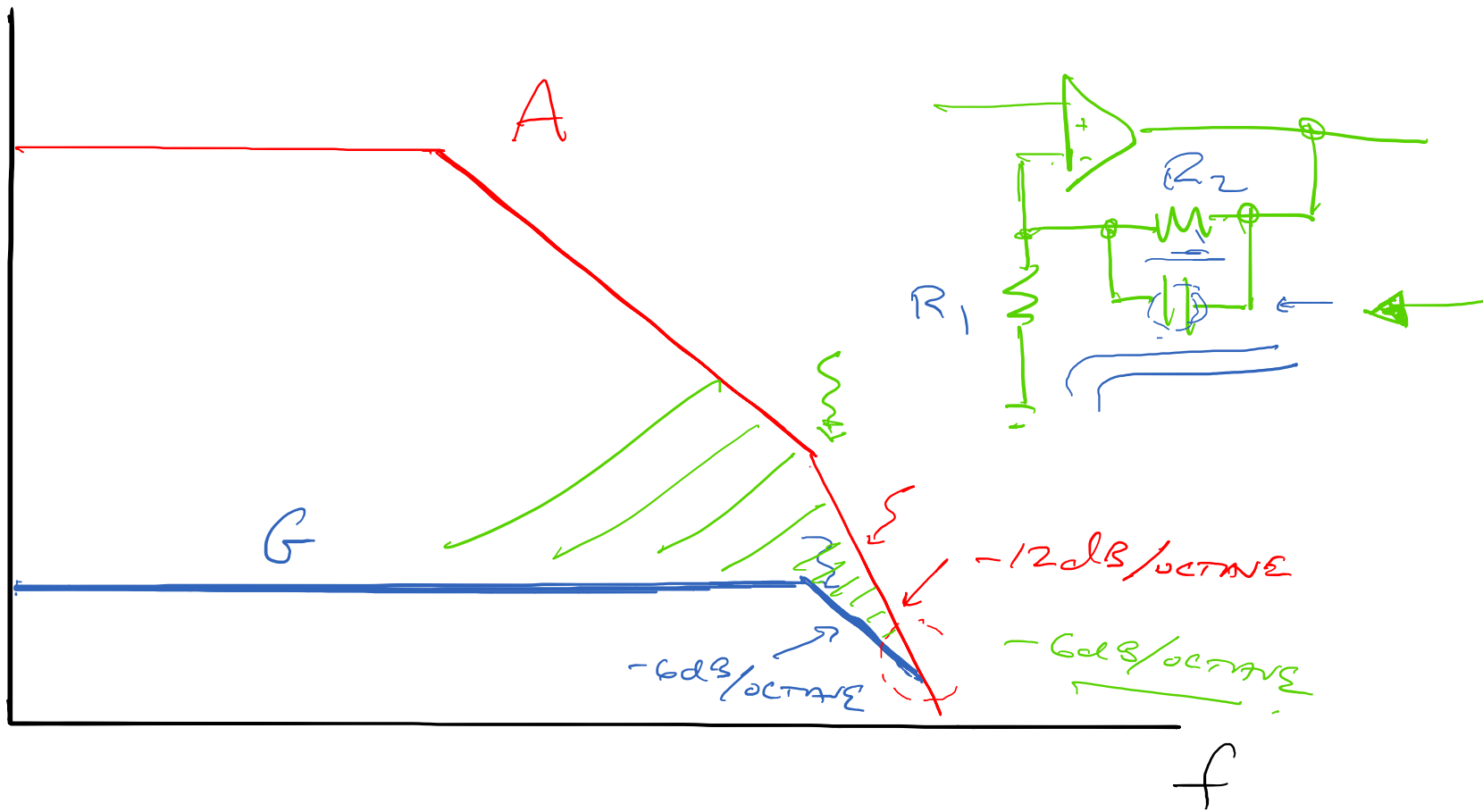
# OP AMP STABILITY



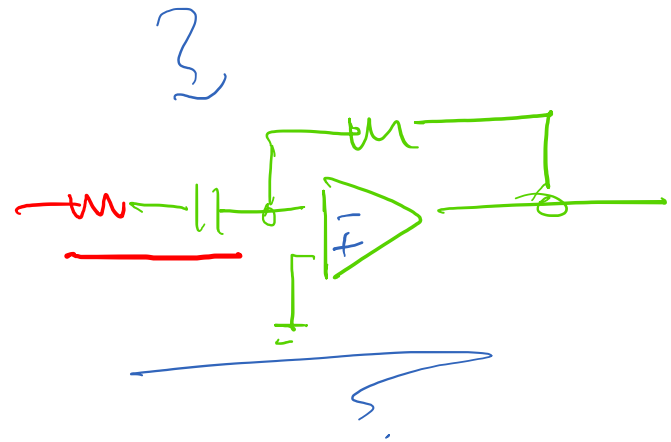
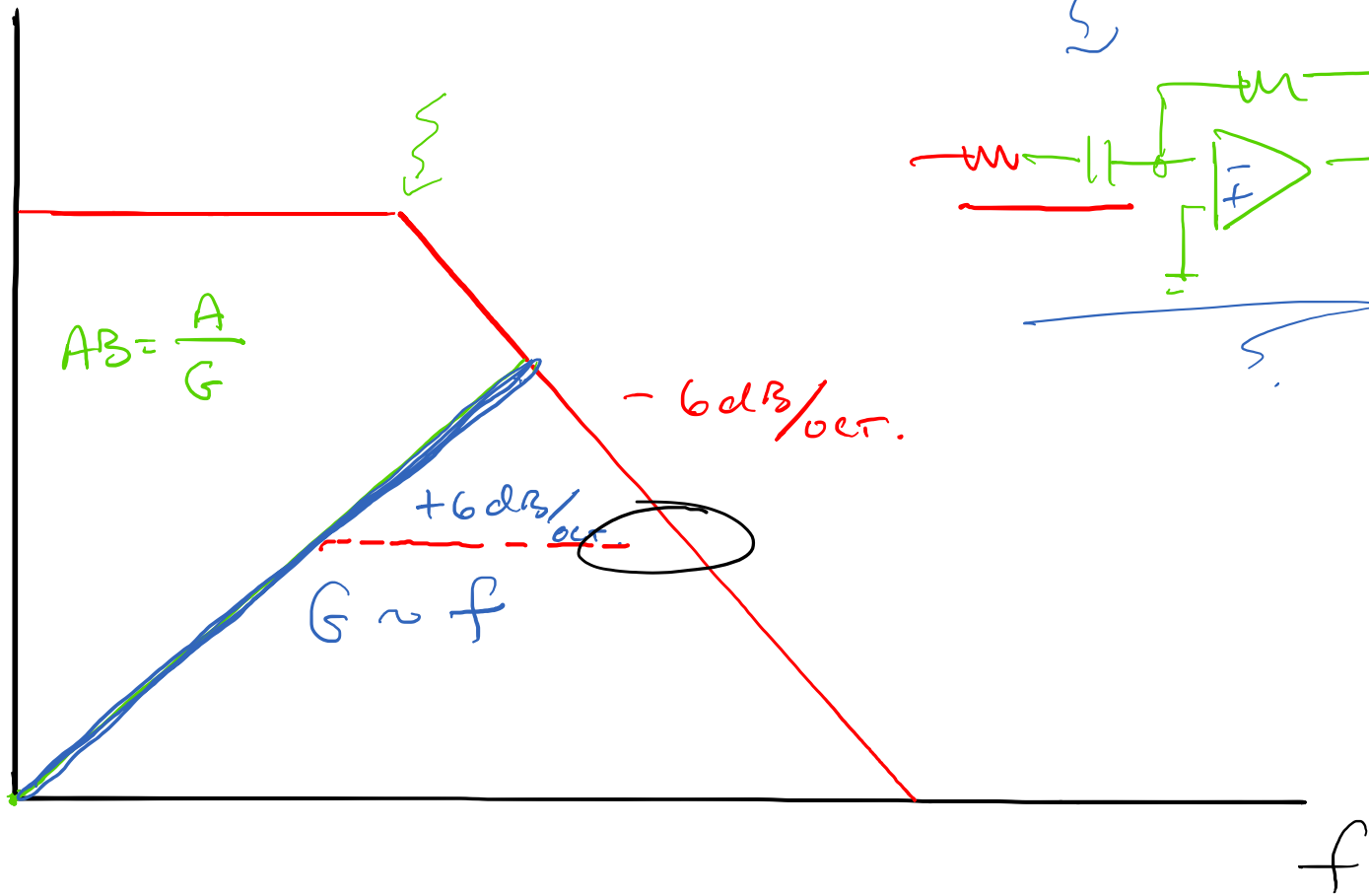
# OP AMP STABILITY



# OP AMP STABILITY



# OP AMP STABILITY



# FOURIER THEORY

CONSIDER PERIODIC SIGNAL

$$V(t \pm T) = V(t)$$

FUNDAMENTAL (ANGULAR) FREQUENCY  $\omega_0 = \frac{2\pi}{T}$

$$V(t) = \frac{a_0}{2} + \sum_{n=1}^{\infty} \left[ a_n \cos n\omega_0 t + b_n \sin n\omega_0 t \right]$$

USE ORTHOGONALITY OF  $\sin/\cos$  TO SOLVE

FOR  $a_n, b_n$

$$\int_{-T/2}^{T/2} \cos n\omega_0 t \cos m\omega_0 t dt = \frac{T}{2} \delta_{nm}$$

$$\int_{-T/2}^{T/2} \sin n\omega_0 t \sin m\omega_0 t dt = \frac{T}{2} \delta_{nm}$$

$$\int_{-T/2}^{T/2} \sin n\omega_0 t \cos m\omega_0 t dt = 0$$



$$a_n = \frac{2}{T} \int_{-T/2}^{T/2} v(t) \cos n\omega_0 t dt \quad \leftarrow$$

$$b_n = \frac{2}{T} \int_{-T/2}^{T/2} v(t) \sin n\omega_0 t dt$$

CONSIDER ODD/EVEN SYMMETRY OF WAVEFORM

ODD: ONLY  $\sin$  COMPONENTS

EVEN: ONLY  $\cos$  COMPONENTS

OR// USE COMPLEX NOTATION

$$\underline{v(t)} = \sum_{\underline{n=-\infty}}^{\infty} \underline{c_n} e^{j n \omega_0 t}$$

$$c_{-n} = c_n^*$$

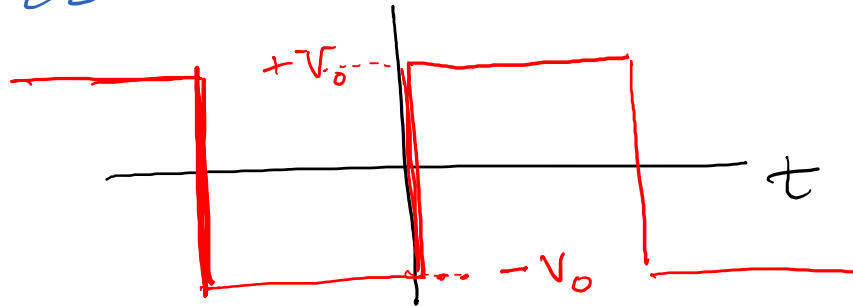
ENSURES  $v(t)$  REAL

ORTHOGONALITY:

$$\int_{-T/2}^{T/2} e^{j(n-m)\omega_0 t} dt = T \delta_{nm}$$

$$\Rightarrow c_n = \frac{1}{T} \int_{-T/2}^{T/2} v(t) e^{-j n \omega_0 t} dt$$

EXAMPLE

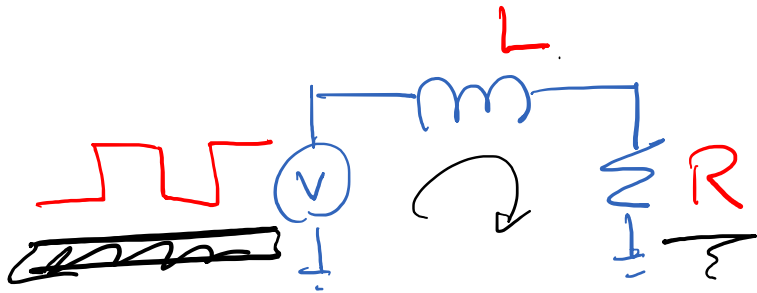


$$c_n = \frac{2}{T} \int_0^{T/2} v_0 e^{-jn\omega_0 t} dt$$

$$c_n = \frac{2}{T} v_0 \left( \frac{-1}{jn\omega_0} \right) \left( e^{-jn\omega_0 T/2} - 1 \right) = \frac{2v_0}{\pi j} \frac{1}{n}$$

$$v(t) = \frac{2v_0}{\pi j} \sum_{n=1}^{\infty} \frac{1}{n} e^{jn\omega_0 t}$$

$$e^{jx} = \cos x + j \sin x$$



$$\underline{Z = R + j\omega L}$$

Solve for  $V_R$

$$\underline{I} = \frac{V}{Z} = \frac{2V_0}{\pi j} \sum_{n \text{ odd}} \frac{1}{n[R + jn\omega_0 L]} e^{jn\omega_0 t}$$

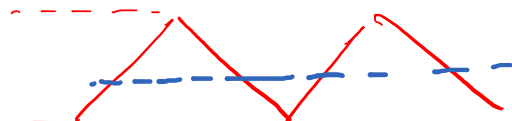
$$\underline{V_R} = \frac{2V_0}{\pi} \sum \frac{1}{-n^2\omega_0^2 L^2 + jn} e^{jn\omega_0 t} \quad ; \quad \underline{\tau = L/R}$$



TAKE  $\omega_0 \tau \gg 1$

$$V_R \approx \frac{2V_0}{\pi} \sum_{n \text{ odd}} \left( -\frac{1}{n^2 \omega_0 \tau} \right) e^{\int_0^{n\omega_0 t} \dots}$$

$$\pm \frac{\pi}{2} \frac{V_0}{\omega_0 \tau}$$



$$V_R \approx \frac{1}{\tau} \int V_{in} dt$$

# FOURIER TRANSFORM

$$v(t) = \sum c_n e^{j n \omega_0 t}$$

$$\text{LET } \omega = n \omega_0 ;$$

TAKE  $\omega_0 \rightarrow 0$  WITH

$$v(t) = \sum c_n e^{j \omega t} \frac{T}{2\pi} \Delta \omega$$

$$\frac{T \Delta \omega}{2\pi} = 1$$

$$\underline{v(t)} = \frac{1}{2\pi} \int_{-\infty}^{\infty} \underbrace{c_n T}_{c_n \cdot T} e^{j \omega t} d\omega$$

$$c_n \cdot T \leftrightarrow \tilde{v}(\omega)$$

FOURIER TRANSFORM

$$v(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \tilde{v}(\omega) e^{j\omega t} d\omega$$

---

FOURIER  
X'FORM

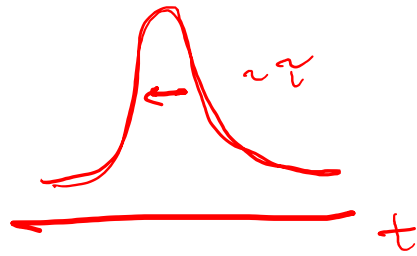
$$\tilde{v}(\omega) = \int_{-\infty}^{\infty} v(t) e^{-j\omega t} dt$$

---

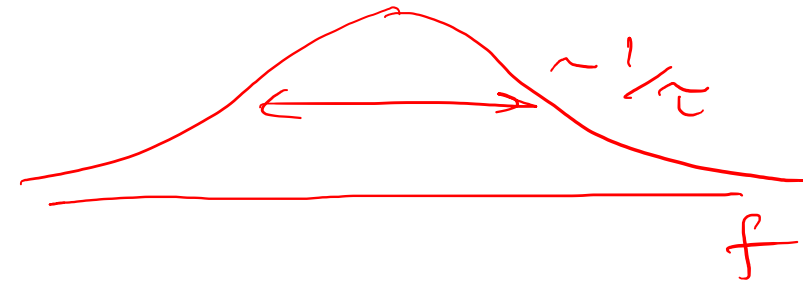
INVERSE  
F. T.

$$v(t) = v_0 e^{-t^2/\tau^2}$$

GAUSS, ADI



$$\tilde{v}(\omega) = \sqrt{\pi} v_0 \tau e^{-(\omega\tau/2)^2}$$



$$v(t) = v_0 e^{-|t|/\tau}$$

EXP. DECAY



$$\tilde{v}(\omega) = \frac{2 v_0 \tau}{1 + j\omega\tau}$$

LORENZIANO  
T?



# EXAMPLE

ARBITRARY



ENERGY COUPLED TO MODE ?

FIRST TAKE

$$I(t) = \underbrace{Q}_{\downarrow} \delta(t)$$

$$V(t) = \frac{Q}{C} \omega_0 \omega_0 t$$

LINEAR RESPONSE THEORY.

GREEN'S FUNCTION /  
IMPULSE RESPONSE.

FOR ARBITRARY  $I(t)$ ,

$$V(t) = \frac{1}{C} \int_{-\infty}^t \underbrace{I(t')}_{\leftarrow} \underbrace{\omega_0 [\omega_0 (t - t')]}_{\leftarrow} dt'$$



$$\underline{V(t)} = \frac{1}{C} \operatorname{Re} \left\{ e^{j\omega_0 t} \int_{-\infty}^t I(t') e^{-j\omega_0 t'} dt' \right\}$$

TAKE  $t \rightarrow \infty$  LOOK LONG AFTER  $I(t) \rightarrow 0$

→ ENERGY STORED IN MODE?

$$\underline{E} = \frac{1}{2} C V_{\max}^2 = \frac{1}{2C} \left| \tilde{I}(\omega_0) \right|^2$$

LOOKS LIKE  
CAPACITOR  
ENERGY

$$\left. \right\} \frac{Q^2}{2C}$$

DIMENSIONALITY,

$$\tilde{I}(\omega_0) \rightarrow Q$$