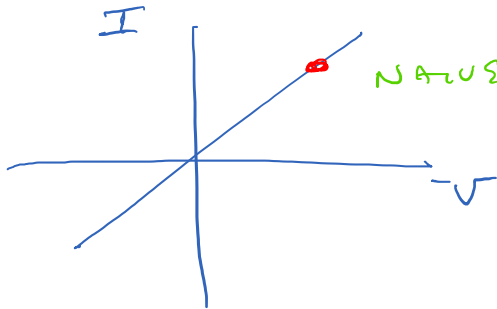


PHASE DETECTOR

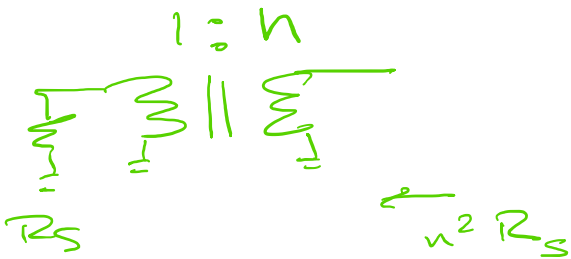
e.g. RESISTANCE THERMOMETRY w/ LOW-LEVEL EXCITATION



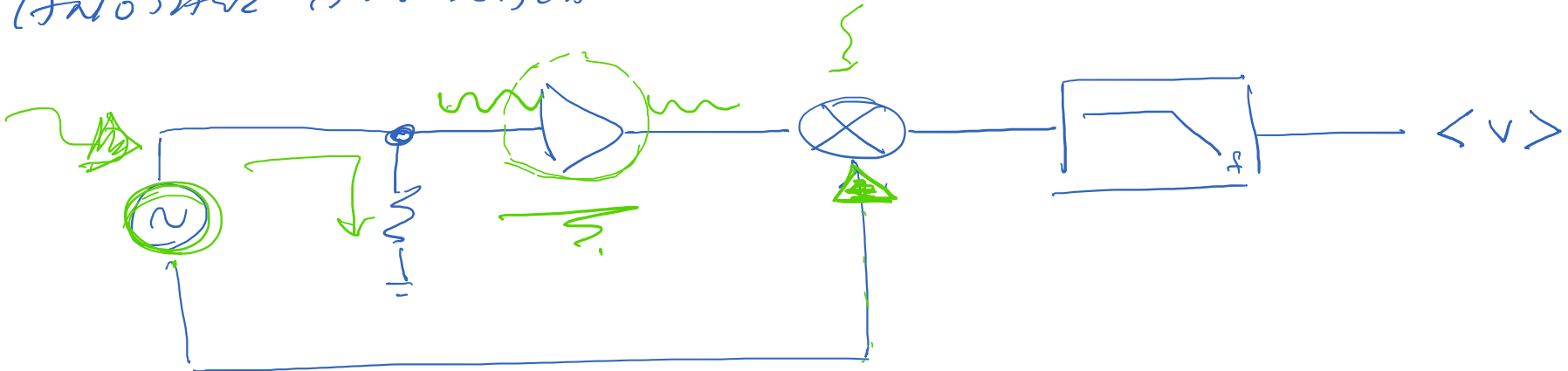
NATURAL APPROACH = BIAS w/ CURRENT,
MEASURE VOLTAGE

Problems :

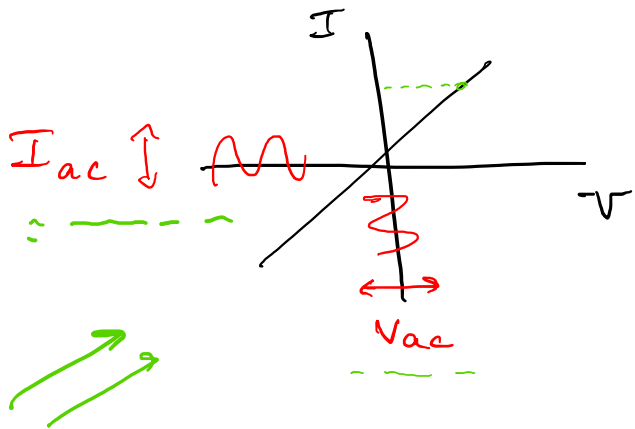
- ① $1/f$ NOISE OF AMP
- ② LOW-FREQUENCY DRIFT
- ③ $R_S \neq R_{N, OPT.}$



ANOTHER APPROACH



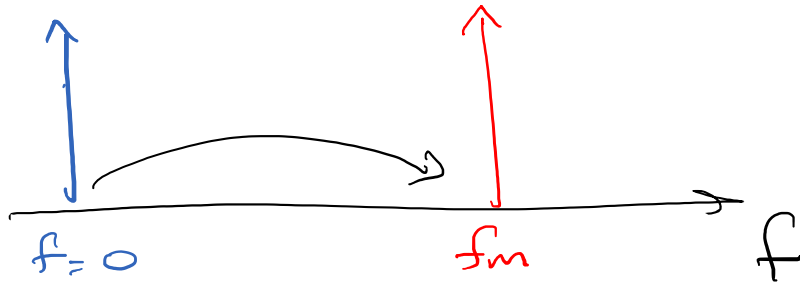
MODULATE EXCITATION @ NONZERO FREQUENCY f_0
 → DETECT IN NARROW BAND AROUND f_0



→ $V_{ac} = R_{0YN} \cdot I_{ac}$

$v(t) = R_{0YN} \cdot I_0 \cos \omega_m t$

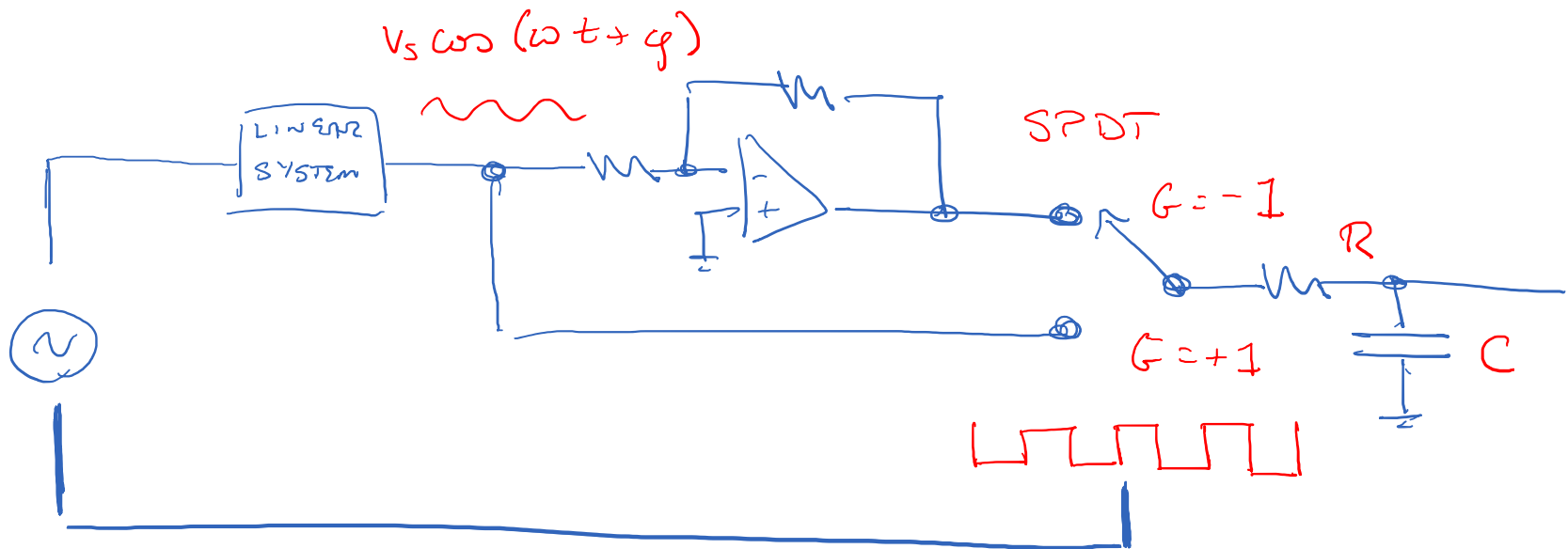
WHAT DOES THIS ACCOMPLISH ?



→ ESCAPE $1/f$ NOISE



ALSO, CAN NOW TRANSFORM SOURCE IMPEDANCE TO OPTIMALLY NOISE MATCH.



POSSIBILITIES:

IN PHASE



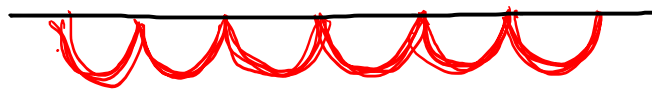
$$\langle v_o \rangle > 0$$

90° SHIFT



$$\langle v_o \rangle = 0$$

180° SHIFT



$$\langle v_o \rangle < 0$$

Assume $RC \gg 2\pi/\omega_m \rightarrow$ JUST LOOK @
DC PART OF OUTPUT



$$\text{LOOK @ } \langle v_s \cos(\omega t + \phi) \rangle \Big|_0^{\pi/\omega} - \langle v_s \cos(\omega t + \phi) \rangle \Big|_{\pi/\omega}^{2\pi/\omega}$$

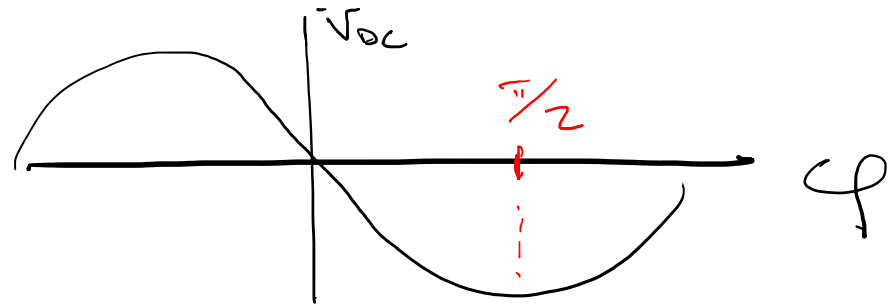
$$= \frac{\omega}{2\pi} v_s \left\{ \int_0^{\pi/\omega} \cos(\omega t + \phi) dt - \int_{\pi/\omega}^{2\pi/\omega} \cos(\omega t + \phi) dt \right\}$$

$$= \frac{v_s}{2\pi} \left\{ \sin(\omega t + \phi) \Big|_0^{\pi/\omega} - \sin(\omega t + \phi) \Big|_{\pi/\omega}^{2\pi/\omega} \right\}$$

$$= \frac{v_s}{2\pi} \left\{ 2 \sin(\pi + \phi) - \sin \phi - \sin(\phi + 2\pi) \right\}$$

$$\boxed{V_{DC} = -\frac{2v_s}{\pi} \sin \phi}$$

$$V_{oc} = -\frac{2v_s}{\pi} \sin \phi$$



FOR $\omega_s \neq \omega_m$

$$v_{out} = -\frac{2v_s}{\pi} \sin \Delta \omega t$$

